AI-BASED AND DATA-DRIVEN ANALYSIS OF PANDEMIC DATA

Sobhan Moazemi

AI & Data Science Team



March 14, 2024 - University of Koblenz

Seite 1

<u>sobhan.moazemi@scai.fraunhofer.de</u>

holger.froehlich@scai.fraunhofer.de

AI & DATA SCIENCE GROUP

Mission: Bringing Better Treatments to the Right Patients





Seite 2

Introduction

Background



Figure 1. Outbreak of COVID-19 pandemic and number of worldwide deaths^[1,2]

- Lack of vaccination and effective treatment.
- Reporting delays of surveillance data (confirmed cases, hospitalization and deaths) for tracking pandemic waves;
 Countries with lack of surveillance capacity
- COVID-19 pandemic has affected healthcare around the world.
- The availability of a reliable, real-time indicator of pandemic would aid in timing public health interventions.

AI-DAS's Contributions

				SCIENTIFIC REPORTS natureresearch	
			<u>Sci Rep.</u> 2023; 13: 20780. Published online 2023 Nov 27. doi: <u>10.1038/s4</u> :	<u> 1598-023-48096-3</u>	PMCID: PMC10682010 PMID: <u>38012282</u>
	Early alert model for pandemic situation	n	Development of an early alert m Dangi Wang, ^{№1} Manuel Lentzen, ^{1,2} Jonas Botz, Edward Thommes, ⁴ Laurent Coudeville, ⁴ and H > Author information > Article notes > Copyright a	nodel for pandemic situations ^{1,2} <u>Diego Valderrama</u> , ^{1,2} <u>Lucille Deplante</u> , ³ <u>Ju</u> tolger Fröhlich ^{®1,2} and License information <u>PMC Disclaimer</u>	s in Germany ules Perrio, ³ Marie Génin, ³
•	ExMedBERT: a Transformer-based mo for structured EHRs	del	 > IEEE J Biomed Health Inform. 2023 Sep;27(9):4548-4558. doi: 10.1109/ Epub 2023 Sep 6. A Transformer-Based Model Trained of Claims Data for Prediction of Severe Co Disease Progression Manuel Lentzen, Thomas Linden, Sai Veeranki, Sumit Madan, Diether Krat Holger Frohlich PMID: 37347632 DOI: 10.1109/JBHI.2023.3288768 Artificial Intelligence in the Life Sciences Volume 1, December 2021, 100020 	JBHI.2023.3288768. In Large Scale OVID-19 mer, Werner Leodolter,	
•	Drug repositioning for COVID-19	Research Article Machin COVID- of Anti Thomas Linder Lauren Nicole Julia Lanznaste Torsten Feldt ^k Jörg Janne Veh	he Learning Based Prediction of -19 Mortality Suggests Repositioning cancer Drug for Treating Severe Cases $a^{0^{b^{*}}} \otimes a$, Frank Hanses ^{c q #} , Daniel Domingo-Fernández ^q , DeLong ^{0, b} , Alpha Tom Kodamulli ⁹ , Jochen Schneider ⁴ , Maria J.G.T. Vehreschild ⁶ , er ^f , Maria Madeleine Ruethrich ^q , Stefan Borgmann ^h , Martin Hower ¹ , Kai Wille ¹ , Siegbert Rieg ¹ , Bernd Hertenstein ¹ , Christoph Wyen ^m , Christoph Roemmele ⁿ , reschild ^e , Carolin E.M. Jakob ^o , Melanie Stecher ^p Holger Fröhlich ^{o b} ^A ^B		



Introduction

Related work

□ Social media posts: creating an early warning system ^[3-15]

Proxy	Techniques	Disease	Country	Training period (COVID-19)
Google Trends; Twitter; News paper feeds;	 Text mining and sentiment analysis (Keyword extraction, TF-IDF, COVID- twitter-BERT, BM, SVM, Naïve Bayes) Anomaly detection (SH_ESD) Statistical tests (Kolmogorov-Sminrvov, Anderson-Darling, Pearson correlations) Linear regression LSTM 	Influenza, dengue, Zika, COVID-19	US, Canada, Australia, Japan, India, India, Colombia, Iran	Winter seasons: December 15, 2018 to January 21, 2019, December 15, 2019 to January 21, 2020; March 1, 2020 to August 21, 2020; January 2020 to March 2020; February 15, 2020 to March 18, 2020; January 22, 2020 to April 3, 2020; Separate COVID-19 pandemic waves

□ Highlights of the study

Multiproxies	Multivariables	Longer training period	Multiple Models
•Google Trends •Twitter	•COVID-19 related German symptoms	•January 2020 to June 2022	•log linear regression model •Random Forest/LSTM



Workflow





Seite 6 © Fraunhofer

Slide credits: Danqi Wang

Result – Country-level trend analysis

Visualization of the up and downtrends



Figure 4. Visualization of the event detection procedure applied to Google Trends, Twitter search and Combined P.



Result – Country-level trend analysis

Pairwise event comparison

Lagging correlation between proxies and gold standard



Figure 5. Up/down trend event detection results for pairwise comparisons between COVID-19 proxies(Google Trends, Twitter, Combined P) and gold standards A) RKI confirmed cases; B) RKI hospitalization; C) RKI deaths in Germany.



Result – Country-level trend analysis

Up trend events performance metrics – Combined proxies

Proxy names	Metric	RKI Cases	RKI Deaths	RKI Hospitalization
Twitter	Sensitivity	0.63	0.29	0.56
	Precision	0.63	0.25	0.63
	F1 Score	0.63	0.27	0.59
Google Trends	Sensitivity	0.88	0.57	0.78
	Precision	0.67	0.33	0.58
	F1 Score	0.76	0.42	0.67
Combined P	Sensitivity	0.63	0.43	0.67
	Precision	0.63	0.38	0.75
	F1 Score	0.63	0.40	0.71

Table 3. Sensitivity $(\frac{TP}{TP+TN})$ and precision $(\frac{TP}{TP+FP})$ rates for certain symptom from different proxies as an early indicator for an uptrend in three differentCOVID-19 gold standards (RKI confirmed cases, deaths, and hospitalization)



Alert model generation

Trend forecasting (Random Forest & LSTM)



Figure 6. The workflow of trend forecasting



Result – Country-level trend forecasting

Uptrend forecasting

Comparison of alert models

Α.		RKI confirmed cases						RKI hospitalization				
	Model	Metrics		Uptrends			Model	Metrics		Uptrends		
			Google Trends	Twitter	Combined				Google Trends	Twitter	Combined	
	Random	sensitivity	0.71	1	1		Random	sensitivity	0.88	0.71	0.67	
	Forest	precision	1	0.6	0.67		Forest	precision	1	0.55	0.91	
		F1 score	0.83	0.75	0.8			F1 score	0.94	0.62	0.77	

Table 5. Evaluation metrics of forecasting models (Random Forest) for forecasting uptrend events (out-of-sample period in 2022) ofA) RKI confirmed cases and B) RKI hospitalization



Result – Country-level trend forecasting

Downtrend forecasting

Comparison of alert models

Α.	RKI confirmed cases				В.	RKI hospitalization					
ſ	Model	Metrics		Downtrends			Model	Metrics		Downtrends	
			Google Trends	Twitter	Combined				Google Trends	Twitter	Combined
ſ	Random	sensitivity	1	0.71	0.86		Random	sensitivity	1	0.88	1
	Forest	precision	0.66	0.76	0.81		Forest	precision	0.88	0.88	0.95
		F1 score	0.8	0.74	0.84			F1 score	0.93	0.88	0.97

Table 6. Evaluation metrics of forecasting models (Random Forest) for forecasting downtrend events (out-of-sample period in 2022) ofA) RKI confirmed cases and B) RKI hospitalization



EARLY ALERT MODEL FOR PANDEMIC SITUATION: CONCLUSION

Country- and State-level COVID-19 early warning model in Germany

- Assessment the utility of Google Trends and Twitter (German symptom based time-series data), and their combined indicator.
- Models: Probabilistic based log linear regression model (Trend analysis)
- Random Forest (Trend Forecasting)

Country-level trend analysis

Compared with the result of Kogan et al. [3] in U.S. (an uptrend in COVID-19 infections could be predicted up to 7 days in advance with an accuracy of

~75%), Google Trends got F1 scores of 0.76 for tracking RKI confirmed cases.

Google Trends can predate an increase in RKI confirmed cases and RKI hospitalization by a median of 16 and 19 days.

Country-level trend forecasting

- RKI confirmed cases: Random Forest-Google Trends (uptrend: F1 score of 0.83; downtrend: F1 score of 0.8)
- RKI hospitalization: Random Forest-Google Trends (uptrend: F1 score of 0.94; downtrend: F1 score of 0.93)
- □ Predictive symptoms for predicting up and down trend events of RKI confirmed cases and RKI hospitalization.
- Google Trends contains important information for effectively predicting disease incidence.

AI-DAS's Contributions

Early alert model for pandemic situation

ExMedBERT: a Transformer-based model for structured EHRs

Drug repositioning for COVID-19

SCIENTIFIC REPORTS Sci Rep. 2023; 13: 20780. PMCID: PMC10682010 Published online 2023 Nov 27. doi: 10.1038/s41598-023-48096-3 PMID: 38012282 Development of an early alert model for pandemic situations in Germany Danqi Wang,^{®1} Manuel Lentzen,^{1,2} Jonas Botz,^{1,2} Diego Valderrama,^{1,2} Lucille Deplante,³ Jules Perrio,³ Marie Génin,³ Edward Thommes,⁴ Laurent Coudeville,⁴ and Holger Fröhlich^{XI,2} ► Author information ► Article notes ► Copyright and License information PMC Disclaimer > IEEE J Biomed Health Inform. 2023 Sep;27(9):4548-4558. doi: 10.1109/JBHI.2023.3288768. Epub 2023 Sep 6. A Transformer-Based Model Trained on Large Scale Claims Data for Prediction of Severe COVID-19 **Disease Progression** Manuel Lentzen, Thomas Linden, Sai Veeranki, Sumit Madan, Diether Kramer, Werner Leodolter, Holger Frohlich PMID: 37347632 DOI: 10.1109/JBHI.2023.3288768 Artificial Intelligence in the Life Sciences Volume 1. December 2021. 100020 ELSEVIER Research Article

Machine Learning Based Prediction of COVID-19 Mortality Suggests Repositioning of Anticancer Drug for Treating Severe Cases

 Thomas Linden ^{a,b, #} A
 ≥ , Frank Hanses^{c,q,#}, Daniel Domingo-Fernández^a,

 Lauren Nicole DeLong ^{a,b}, Alpha Tom Kodamulil ^a, Jochen Schneider ^d, Maria J.G.T. Vehreschild ^e,

 Julia Lanznaster ^f, Maria Madeleine Ruethrich ^g, Stefan Borgmann ^h, Martin Hower ^I, Kai Wille^J,

 Torsten Feldt ^k, Siegbert Rieg ^I, Bernd Hertenstein ¹, Christoph Wyen ^m, Christoph Roemmeleⁿ,

 Jörg Janne Vehreschild ^e, Carolin E.M. Jakob ^o, Melanie Stecher ^p...Holger Fröhlich ^{a,b}



Seite 14 © Fraunhofer

Leveraging Clinical Routine Data to Predict Risk of Severe COVID-19 Disease Progression





Development of a Transformerbased model for structured EHRs

- Improved Med-BERT by incorporating further patient information (age, sex, residency / state, medication history)
- Pretrained the model on a large dataset of 3.5 million patients (988 million instances of drugs and diagnoses)
- Developed predictive risk models for forecasting Acute Respiratory Manifestations (ARM) post COVID-19 diagnosis using the refined model
- Validated model effectiveness and accuracy through benchmarks against Random Forest, RETAIN, and XGBoost





ExMed-BERT outperforms RF, RETAIN & XGBoost for predicting acute respiratory manifestation following COVID-19





Slide credits: Manuel Lentzen

Assessing Global Feature Importance using Integrated Gradient Approach: Top 20 Diagnoses and Drugs for ExMed-BERT-GRU





Slide credits: Manuel Lentzen

Understanding Relationships: Bayesian Network Analysis of Morbid Obesity / Angiotensin II Receptor Blockers and Other Diagnoses/Drugs



Slide credits: Manuel Lentzen

EXMEDBERT: CONCLUSION

- We generated customized transformer-based model for structured EHR data
- Risk models developed for ARM endpoint outperform RF, RETAIN and XGBoost models
- Performance enhancement through incorporation of quantitative clinical data
- Identification of several known risk factors as important features for our model
- Transfer learning enables utilization of pre-trained ExMed-BERT model for diverse clinical endpoint predictions



AI-DAS's Contributions

Early alert model for pandemic situation

ExMedBERT: a Transformer-based model for structured EHRs

Drug repositioning for COVID-19

SCIENTIFIC REPORTS natureresearch

<u>Sci Rep.</u> 2023; 13: 20780. Published online 2023 Nov 27. doi: <u>10.1038/s41598-023-48096-3</u> PMCID: PMC10682010 PMID: <u>38012282</u>

Development of an early alert model for pandemic situations in Germany

Danqi Wang,^{®1} Manuel Lentzen,^{1,2} Jonas Botz,^{1,2} Diego Valderrama,^{1,2} Lucille Deplante,³ Jules Perrio,³ Marie Génin,³ Edward Thommes,⁴ Laurent Coudeville,⁴ and Holger Fröhlich^{®1,2}

► Author information ► Article notes ► Copyright and License information PMC Disclaimer

> IEEE J Biomed Health Inform. 2023 Sep;27(9):4548-4558. doi: 10.1109/JBHI.2023.3288768. Epub 2023 Sep 6.

A Transformer-Based Model Trained on Large Scale Claims Data for Prediction of Severe COVID-19 Disease Progression

Manuel Lentzen, Thomas Linden, Sai Veeranki, Sumit Madan, Diether Kramer, Werner Leodolter, Holger Frohlich

PMID: 37347632 DOI: 10.1109/JBHI.2023.3288768



Artificial Intelligence in the Life Sciences Volume 1, December 2021, 100020

Research Article

Machine Learning Based Prediction of COVID-19 Mortality Suggests Repositioning of Anticancer Drug for Treating Severe Cases

 Thomas Linden ° b # Q ≥, Frank Hanses ^c q #, Daniel Domingo-Fernández °,

 Lauren Nicole DeLong ° b, Alpha Tom Kodamullil °, Jochen Schneider ^d, Maria J.G.T. Vehreschild ^e

 Julia Lanznaster ^f, Maria Madeleine Ruethrich ^g, Stefan Borgmann ^h, Martin Hower ^I, Kai Wille ^J,

 Torsten Feldt ^k, Siegbert Rieg ^I, Bernd Hertenstein ^I, Christoph Wyen ^m, Christoph Roemmele ⁿ,

 Jörg Janne Vehreschild ^e, Carolin E.M. Jakob °, Melanie Stecher ^p...Holger Fröhlich ° ^b Q ≅



Seite 21 © Fraunhofer

The Cohort: COVID-19 patients from the Lean European Open Survey on SARS-CoV-2 infected patients

active sites,

European

+00

1

.⊆

patients recruited

2

 \square

9

ermany

J

ove

_

ത

primarily

Overview of patient demographics in LEOSS. test confirmed SARS-CoV Age 18 - 25 years 181 26 - 35 years 472 540 36 - 45 years 907 46 - 55 years 1125 56 - 65 years 981 66 - 75 years 76 - 85 years 1231 242 missing Gender 3229 2218 232 rapid Ethnicity 4225 1195 155 98 6 PCR Country 5411 ~5700 65 40 33 27 from 26 23 19 Spain 15 ata 11 France





Female missing Caucasian missing Asian & Pacific Islander African & African American Hispanic or Latino Germany Turkey Belgium Czechia Latvia Other GBR Italy

Male

Austria

Machine learning can predict mortality with high accuracy



Model prediction performance measured via Uno's C-index on held out test sets (COX = elastic net penalized Cox proportional hazards regression; WEI = elastic net penalized Weibull accelerated failure time regression; XGBSE = XGBoost Survival Embeddings; RSF = Random Survival Forest; DEEPSURV = DeepSurv); (b) model calibration error measured via Integrated Brier Score (IBS) on held out test sets; (c) model prediction performance as function of time on held out test sets with 95% confidence interval, with integrated AUC (iAUC) denoting the mean (standard error) AUC over time. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Feature importances via SHAP values:

- lab measures were the most relevant type of features (23.5% cumulative importance)
- Disease symptoms ranked second (20.5%)
- Comorbidities third (13.2% cumulative importance).
- Comorbidity associated predictors included hypertension, an acute kidney injury, diabetes and dementia

rank	domain	feature	importance
1	Demographic	Age	6.5%
2	Symptoms	Asymptomatic	2.9%
3	Vital	SO2 Oxygen Saturation	2.9%
4	Hemato. Lab	Hemoglobin	2.6%
5	Lab	Troponine T	2.6%
6	Symptoms	Muscle Aches	2.4%
7	Lab	Ferrit	2.4%
8	Lab	CRP	2.3%
9	Hemato. Lab	Platelets	2.2%
10	Demographic	Gender	1.9%
46	Dementia	Comorbidities	0.8%
		Total	29.4%

b)		
Modality	Cumulative Importance	Number of Features
Lab	23.5%	25
Symptoms	20.5%	41
Comorbidities	13.2%	43
Vital	11.2%	11
Hemato. Lab	11.1%	8
Demographic	8.7%	3
Treatments	4.2%	5
CT_Xray	3.1%	12
Urine	2.0%	8
Other	1.6%	2
Smoking	1.0%	2
Total	100%	160



Partial dependence plots for most influential predictors



An asymptomatic Covid-19 infection resulted into a 35% lower mortality risk compared to more severe disease symptoms

For patients with low hemoglobin level or low oxygen saturation mortality risk was even increased by 50%

Prior diagnosis of dementia results into an 15% increased mortality risk after SARS-CoV-2-19 infection (hazard ratio dementia vs. non-dementia: 1.15; 95% CI: [1.08, 1.24])



Seite 24 © Fraunhofer

Anti-cancer drugs Regoratenib and Soratenib help treat COVID-19 patients

- By calculating the overlap of multiple knowledge graphs and subsequent research in GWAS* studies:
- Identified Regorafenib and Sorafenib as potential COVID-19 drugs targeting TYK2 through cellular screening assay for anti-cytopathic effect.
- Regorafenib and Sorafenib were tested in Vero-E6 and Caco2 cell lines against SARS-CoV-2.
- Results shown: percentage inhibition of viral cytopathic effect normalized to Remdesivir as positive control (100%).
- Drug administration occurred 48 or 96 hours post-infection, with stained, washed, and counted cells indicating some toxicity, particularly in Caco2 cells at higher concentrations.c effect compared to Remdesivir
- The slightly negative relative inhibition shown in panel D is caused by plate control differences within plates.





GREAT NEWS: ONGOING CLINICAL TRIAL!

An Observational Study, Called ROCURS, to Learn About COVID-19 Related Outcomes in People With Cancer Who Are Treated With Tyrosine Kinase Inhibitors (TKIs) Including Regorafenib or Sorafenib (ROCURS)

ClinicalTrials.gov ID

NCT05594147

Sponsor
Bayer

Information provided by
Bayer (Responsible Party)

Last Update Posted 1 2023-11-07



Seite 26 © Fraunhofer

DRUG REPOSITIONING FOR COVID-19: CONCLUSION

- Despite vaccination efforts, COVID-19 cases continued to rise globally until 2021, highlighting the need for effective medications against severe cases.
- A machine learning (ML) model was developed to predict COVID-19 mortality using extensive observational data from LEOSS, primarily from German inpatient settings.
- The ML model performs similarly to the established 4C mortality score (from UK) but differs in formulation, focusing on timedependent mortality risk after COVID-19 diagnosis.
- The model identifies dementia as a predictor, suggesting TYK2 as a potential drug target for COVID-19.
- Regorafenib and Sorafenib, anti-cancer drugs, show promise as potential COVID-19 treatments based on cellular screening assays.
- The study demonstrates the utility of ML-based risk models in identifying potential drug targets and treatment options for COVID-19.
- Clinical trials already ongoing to confirm the efficacy of Regorafenib and Sorafenib in treating COVID-19.



Appropriate Solutions for Different Phases of COVID-19 Pandemic

- Evaluation of Google Trends and Twitter for symptom-based time-series data
- Models: Probabilistic log linear regression and Random Forest for trend analysis and forecasting
- Comparison with Kogan et al. in the U.S., showcasing F1 scores for tracking RKI confirmed cases
- Google Trends predated RKI confirmed cases and hospitalizations by a median of 16 and 19 days
- Customized transformer-based model for structured EHR data and ARM endpoint risk modeling
- Transfer learning enables utilization of pre-trained ExMed-BERT model for diverse clinical endpoint predictions
- Performance enhancement through incorporation of quantitative clinical data
- Identification of several known risk factors as important features for our model
- Identification of TYK2 as a potential drug target for COVID-19 using ML predictions
- Potential COVID-19 treatments: Regorafenib and Sorafenib, based on cellular screening assays
- Ongoing clinical trialds for Regorafenib and Sorafenib efficacy
- Demonstration of ML-based risk models' utility in identifying drug targets and treatment options for COVID



Seite 28 © Fraunhofer

Early Alert Model

Clinical Endpoint

Prediction

Repositioning

ACKNOWLEDGEMENTS



AI & Data Science Team @ Fraunhofer SCAI

Former Associates



Mohamed Aborageh	Tim Ada
Jonas Botz	Sabyasa
Jannis Guski	Tom Hä
Sophia Krix	Kiril Klei
Manuel Lentzen	Johanna
Sumit Madan	Lennart
Tamara Raschka	Konrad
Diego Valderrama	Georgv
Sobhan Moazemi	Sebastia

Holger Fröhlich

ams achi Patyoshi hnel in (guest) a Driever Carsten-Behrens Gerischer . Arnim an Schwick

Danqi Wang

Thomas Linden





sobhan.moazemi@scai.fraunhofer.de

holger.froehlich@scai.fraunhofer.de















References

[1] <u>https://upload.wikimedia.org/wikipedia/commons/b/b3/COVID-19-outbreak-timeline.gif</u> (access on 17.09.2022)

[2] https://ourworldindata.org/explorers/coronavirus-data-explorer (access on 07.02.2023)

[3] N.E. Kogan, et al. An early warning approach to monitor COVID-19 activity with multiple digital traces in near real time. Sci. Adv. 7, eabd6989 (2021).

[4] V. Madhur, et al. Google Search Trends predicting disease outbreaks: an analysis from India. Healthc Inform Res. 24(4):300-308 (2018).

[5] F. Dean. Short-term forecasting of the COVID-19 pandemic using Google Trends data: Evidence from 158 countries. Applied Econometrics. 1-20 (2020).

[6] Ayyoubzadeh SM, Ayyoubzadeh SM, Zahedi H, Ahmadi M, Kalhori SRN. Predicting COVID-19 incidence through analysis of google trends data in Iran: data mining and deep learning pilot study. JMIR Public Health Surveill. (2020) 6:e18828. doi:10.2196/18828.

[7] Ortiz-Martínez Y, Garcia-Robled JE, Vásquez-Castañeda DL, Bonilla-Aldana DK, Rodriguez-Morales AJ. Can Google R[©] trends predict COVID-19 incidence and help preparedness? The situation in Colombia. Travel Med Infect Dis. (2020) 37:101703. doi:10.1016/j.tmaid.2020.101703.

[8] M. J. Pau, et al. Twitter improves influenza forecasting. PLOS Curr. 6, ecurrents.outbreaks.90b9ed0f59bae4ccaa683a39865d9117 (2014).

[9] R. Nagar, et al., A case study of the New York City 2012-2013 influenza season with daily geocoded Twitter data from temporal and spatiotemporal perspectives. J. Med. Internet Res. 16, e236 (2014).

[10] A. Z. Klein, et al. Toward using Twitter for tracking COVID-19: A natural language processing pipeline and exploratory data set. J. Med. Internet Res. 23, e25314 (2021).

[11] Vu Tran, et al. Tweet analysis for enhancement of COVID-19 epidemic simulation: a case study in Japan. Front. Public Health. (2022).

[12] R. Lamsal, et al. Twitter conversations predict the daily confirmed COVID-19 cases. Applied Soft Computing. 2206.10471v2 (2022).

[13] S. Yousefinaghani, et al. The assessment of Twitter's potential for outbreak detection: avian influenza case study. Sci. Rep. 9:18147(2019).

[14] A. Mavragani. Tracking COVID-19 in Europe: Infodemiology Approach. JMIR Public Health Surveill. 6(2):e18941(2020).

[15] Y.M. Zhang, et al. An intelligent early warning system of analyzing Twitter data using machine learning on COVID-19 surveillance in the US. Expert Systems with Applications 198(2022).

[16] Cleveland, R. B., Cleveland, W. S., McRae, J. E., and Terpenning, I. (1990). STL: A seasonal-Trend Decomposition Procedure Based on Loess. Journal of Official Statistics, 6(1):3–73.

[17] R.J. Hyndman, G. Athanasopoulos. Forecasting: principles and practice, 3nd edition, Otexts: Melbourne, Australia. Otexts: com/fpp2.

